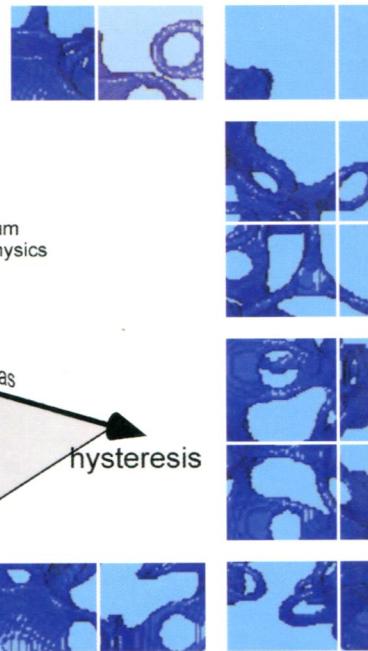


Series in Soft Condensed Matter **Vol. 6**



**Stephan Herminghaus**

# **WET GRANULAR MATTER**

## A Truly Complex Fluid



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