



GLASSY DISORDERED SYSTEMS

**Glass Formation and Universal
Anomalous Low-Energy Properties**

Michael I. Klinger

A black and white micrograph showing a disordered arrangement of small, dark, spherical particles. The particles are scattered across the field of view, with some appearing in small clusters and others in isolation. The background is light gray with a fine, regular grid pattern.

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Glass Formation and Universal Anomalous Low-Energy Properties (Soft Modes)

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CONTENTS

Preface	v
1. Fundamental Properties of Glasses	1
1. General Description of Glasses and Glass Transition	3
1.1. Metastability and disorder. Types of glasses	3
1.2. Qualitative description of glass (liquid-to-glass) transition	5
1.3. Kinetic and thermodynamic properties	9
1.4. Slow relaxation processes	12
2. Models of Glassy (Topologically Disordered) Structures	15
2.1. Characteristics of glassy structures	15
2.2. Homogeneous (ideal) models	18
2.3. Inhomogeneous (cluster) models	23
3. Some Theoretical Models of Glass Transition	27
3.1. Vogel–Fulcher relation and “entropy crisis”	27
3.2. Role of configurational entropy, free-volume effects and “defects” diffusion	31
3.3. Mode-coupling model: Dynamic liquid-glass transition	40
4. Kohlrausch–William–Watt (KWW) Relaxation	47
4.1. General features of slow relaxation processes	47
4.2. Parallel-diffusion relaxation models	49

4.3.	Correlated, hierarchically constrained, relaxation models	52
4.4.	Concluding remarks	56
II.	Anomalous Low-Energy Dynamics of Glasses	59
5.	Origin of Anomalous Low-Energy Properties of Glasses	61
6.	Experimental Background for Anomalous Low-Energy Atomic Dynamics	69
6.1.	Very low temperatures and frequencies	69
6.2.	Moderately low temperatures and frequencies	82
7.	Soft-Mode Model of Low-Energy Atomic Dynamics	93
7.1.	Atomic soft modes and related potentials	94
7.2.	Probability distribution densities	105
7.3.	Low-energy excitations: Density of states and concentration	112
7.4.	Interaction of soft-mode excitations with acoustic phonons	117
8.	Soft-Mode Excitations of Very Low and “Intermediate” Energies	123
8.1.	Soft-mode tunneling states (independent two-level systems)	124
8.2.	Soft-mode excitations of “intermediate” energies	133
9.	Tunneling States as Very Low Energy Limit Case	141
9.1.	Standard tunneling model: Independent two-level systems	141
9.2.	Advanced tunneling model: Interacting two-level systems	150
9.2.1.	Mean-field approximation: “Spectral diffusion”	150
9.2.2.	Many-body effects: Collective excitations	157

10. Soft-Mode Excitations of Moderately-Low Energies (Boson Peak)	165
10.1. Ioffe–Regel crossover for acoustic phonons as origin of boson peak	165
10.2. Independent soft-mode vibrational excitations	169
10.3. Total vibrational density of independent soft-mode states	178
10.4. Generalization for interacting harmonic excitations	184
10.5. Total vibrational density of states: dynamic properties	188
10.6. Width (attenuation) of acoustic phonons	195
10.7. Thermal vibrational properties of glasses	199
11. On Universal and Non-Universal Dynamic Properties of Glasses	207
11.1. Very low temperatures and frequencies	207
11.1.1. On universality of basic distributions in ATM	208
11.1.2. On universality of soft-mode distribution in SMM	217
11.2. Moderately low temperatures and frequencies	217
12. Other Models for Glasses with High Frequency Sound	223
12.1. Theoretical mode-coupling model	225
12.2. Theoretical random-matrix model	232
12.3. Comparison with the soft-mode model	236
13. Recent Models for Glasses with No High-Frequency Sound	241
13.1. Boson peak: Ioffe–Regel crossover at elastic acoustic scattering	242
13.2. Dynamic and thermal anomalies at elastic acoustic scattering	245
13.3. Boson peak due to spatially random springs constants	249
13.4. Nakayama model: Boson peak vs strongly localised modes	251

14. Anomalous Electron Properties of Semiconducting Glasses	253
14.1. Basic experimental data	253
14.2. Negative- U centres: Anderson model	254
14.3. Street–Mott and Kastner–Adler–Fritzsche models	257
14.4. Qualitative analysis of negative- U centres	260
15. Soft-Mode Model of Localized Electron States in the Glasses	267
15.1. General considerations	267
15.2. Model of negative- U centres: Basic relations and approximations	268
15.3. Adiabatic potentials and electron energy	271
15.4. Basic features of self-trapped states and negative- U centres	277
15.5. Density of states and thermal equilibrium properties	282
15.6. Concluding remarks	287
16. Additional Manifestations of Soft Modes in Glasses	289
16.1. Negative- U centres model of photostructural changes in semiconducting glasses	289
16.2. Gap-light frequency dependence	301
16.3. Temperature dependence	303
17. Summary, Conclusions and Problems	305
Appendix A. Convolution of Soft-Mode Vibrational DOS and Transformation Kernel in the DOS of BP and HFS Excitations	309
References	315
Index	325