Rainer Kimmich

Principles of Soft-Matter Dynamics

Basic Theories, Non-invasive Methods, Mesoscopic Aspects

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